

**2B22**  
**QUANTUM PHYSICS &**  
**QUANTUM FOUNDATIONS OF ASTROPHYSICS**  
**PROBLEMS 5**

To be handed in by ...

You may use

$$\int_0^\infty r^n e^{-\alpha r} dr = \frac{n!}{\alpha^{n+1}}$$

1. (a) Given that 1 atomic unit of energy is  $4.3598 \times 10^{-18} J$ , calculate the energies of the hydrogen atom in the states with principal quantum number  $n = 2, 3, 4$ .  
(b) Calculate the frequencies in Hertz, and the wavelengths in angstroms, of all the photons that can be emitted by the atom in transitions between these levels.  
(c) A sample of hydrogen atoms is prepared in the  $4p$  state. At how many wavelengths will light subsequently be observed? How would the wavelengths differ if the atoms had been prepared in the  $4s$  state?
2. An excited state of TiIII has two active electrons in the configuration  $3d4p$ . Give the possible values of  $L, S, J$  which may arise, explaining your working.
3. A sample of hydrogen atoms are prepared in the  $3p$  state. The probability for a transition to the  $2s$  state is given by the expression:

$$P_{3p \rightarrow 2s} = \frac{2.026 \times 10^{18}}{\lambda^3} |\mathbf{M}_{3p \rightarrow 2s}|^2$$

where  $M_{3p \rightarrow 2s}$  is the dipole matrix element for the transition and  $\lambda$  is the wavelength in angstroms.

Assuming emitted radiation is polarized along the  $z$  axis, so  $\epsilon \cdot \mathbf{r} = r \cos \theta$ , calculate the probability for this transition given that  $R_{31} = (\frac{2}{3})^{3/2} r(1-r/6) \exp -r/3$  and  $R_{20} = \frac{2}{2^{3/2}} (1-r/2) \exp -r/2$ .