Ideal Gas Model

- Molecules may be treated as point masses relative to the volume of the system.
- Molecular collisions are elastic, i.e. kinetic energy is conserved.
- Intermolecular forces of attraction and repulsion have negligible on the molecular motion.

Ideal Gas Assumptions

- The number of molecules in the gas is large, and the average separation between the molecules is large compared with their dimensions
 - The molecules occupy a negligible volume within the container
 - This is consistent with the macroscopic model where we assumed the molecules were pointlike

Ideal Gas Assumptions, 2

- The molecules obey Newton's laws of motion, but as a whole they move randomly
 - Any molecule can move in any direction with any speed
 - At any given moment, a certain percentage of molecules move at high speeds
 - Also, a certain percentage move at low speeds

Ideal Gas Assumptions, 3

- The molecules interact only by short-range forces during elastic collisions
 - This is consistent with the macroscopic model, in which the molecules exert no long-range forces on each other
- The molecules make elastic collisions with the walls
- The gas under consideration is a pure substance
 - All molecules are identical

Ideal Gas Notes

- An ideal gas is often pictured as consisting of single atoms
- However, the behavior of molecular gases approximate that of ideal gases quite well
 - Molecular rotations and vibrations have no effect, on average, on the motions considered

Pressure and Kinetic Energy

- Assume a container is a cube
 - Edges are length d
- Look at the motion of the molecule in terms of its velocity components
- Look at its momentum and the average force



Pressure is the amount of momentum that crosses a unit area of the surface per unit time:

$P = 1/A \times d(mv)/dt$

Pressure and Kinetic Energy, 2

- Assume perfectly elastic collisions with the walls of the container
- The relationship between the pressure and the molecular kinetic energy comes from momentum and Newton's Laws



Pressure and Kinetic Energy, 3

• The relationship is

$$P = \frac{2}{3} \left(\frac{N}{V} \right) \left(\frac{1}{2} m \overline{v^2} \right)$$

 This tells us that pressure is proportional to the number of molecules per unit volume (*N*/*V*) and to the average translational kinetic energy of the molecules

Pressure and Kinetic Energy, final

- This equation also relates the macroscopic quantity of pressure with a microscopic quantity of the average value of the square of the molecular speed
- One way to increase the pressure is to increase the number of molecules per unit volume
- The pressure can also be increased by increasing the speed (kinetic energy) of the molecules

Molecular Interpretation of Temperature

• We can take the pressure as it relates to the kinetic energy and compare it to the pressure from the equation of state for an ideal gas

$$P = \frac{2}{3} \left(\frac{N}{V} \right) \left(\frac{1}{2} m \overline{v^2} \right) = N k_{\rm B} T$$

• Therefore, the **temperature** is a direct measure of the **average molecular kinetic energy**

Molecular Interpretation of Temperature, cont

 Simplifying the equation relating temperature and kinetic energy gives

$$\frac{1}{2}m\overline{v^2} = \frac{3}{2}k_{\rm B}T$$

 $1 - \frac{1}{2}$ 1, ...

• This can be applied to each direction,

$$\frac{-mv_x}{2} = \frac{-\kappa_B I}{2}$$

with similar expressions for v_y and v_z