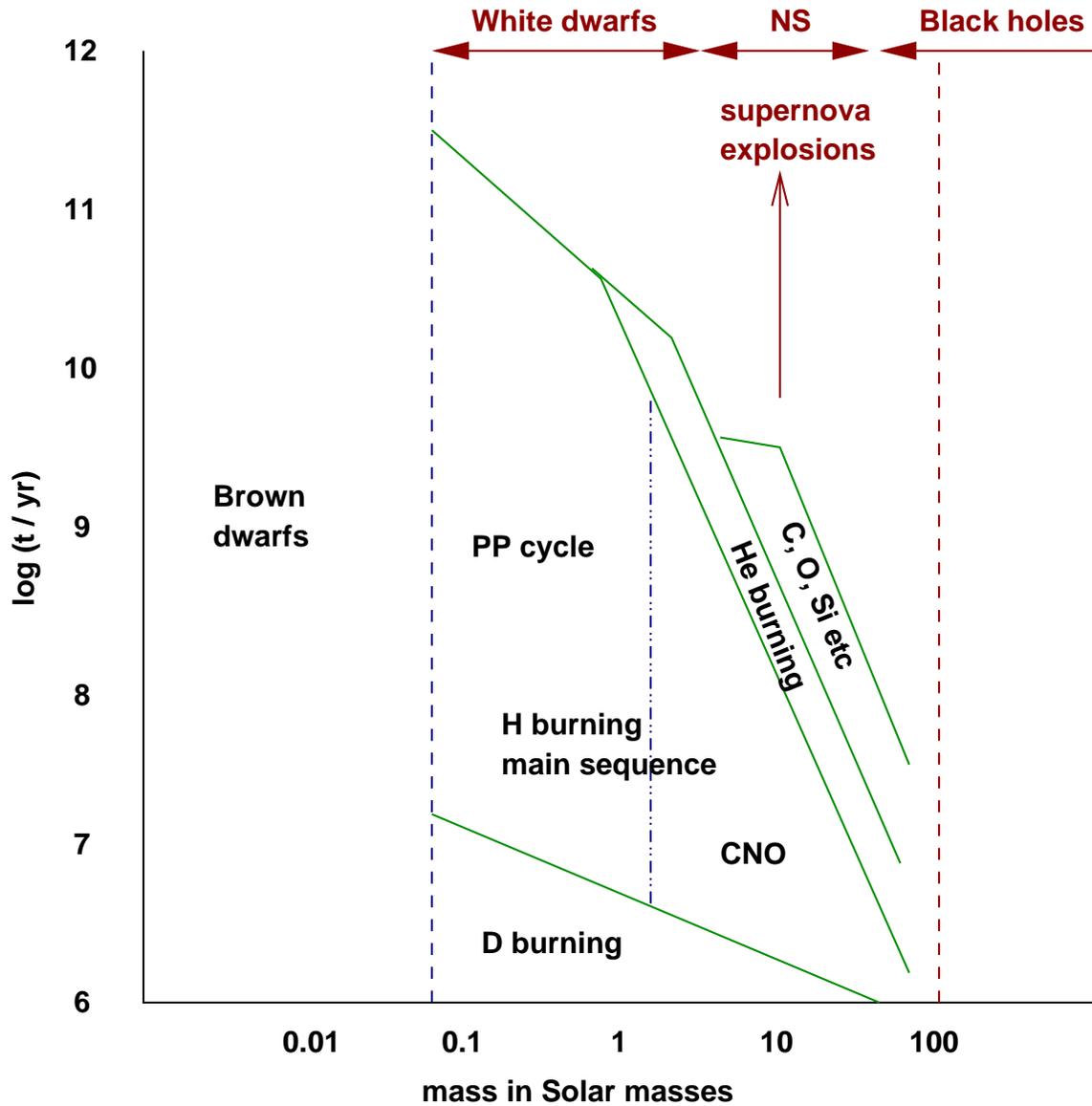


# Post-main-sequence evolution



Need to consider:

- Track in HR diagram (very luminous).
- Mass loss (source of uncertainty).
- Final endpoint, WD, NS or black hole?

## Summary of probable endpoints

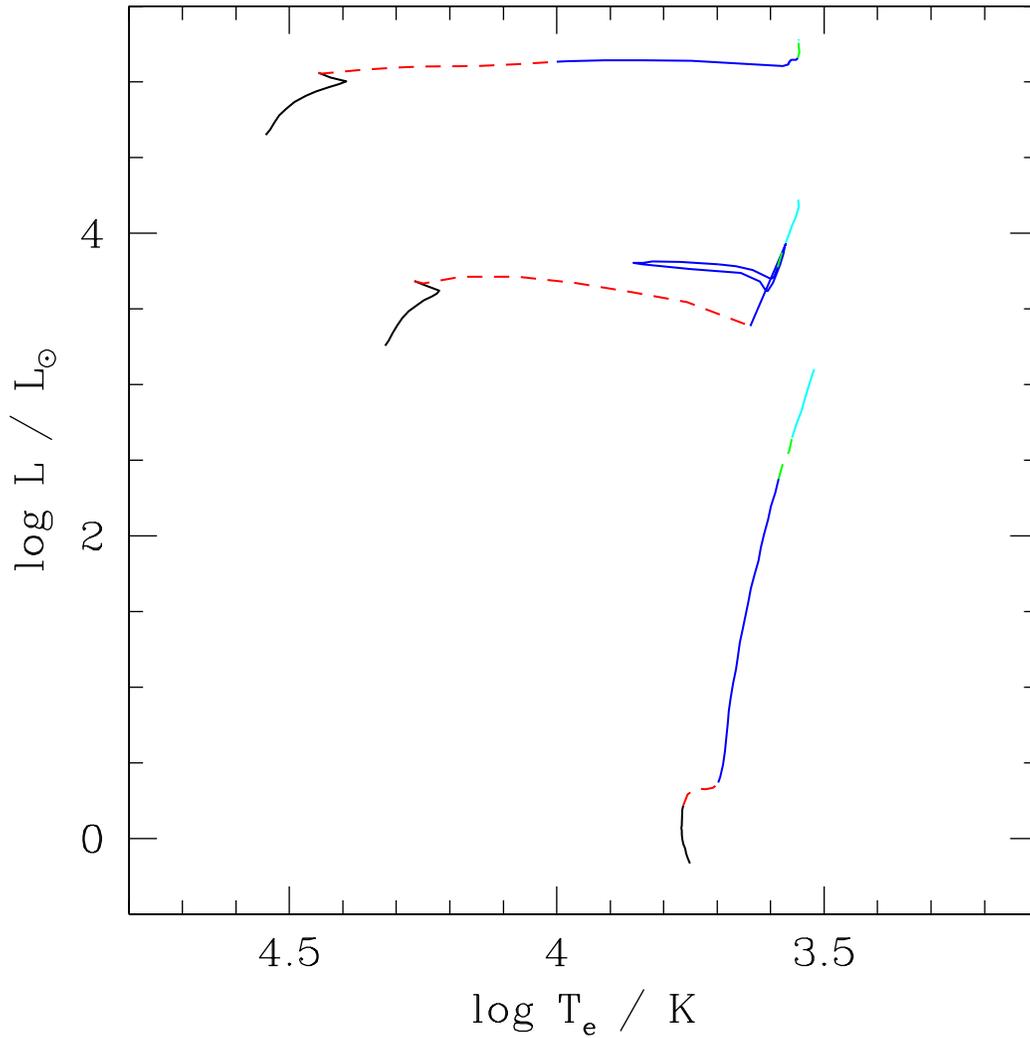
Uncertainties in the boundaries due to eg,

- Treatment of convection.
- At high masses, extent of stellar winds.

$M < 0.08M_{\odot}$	Brown dwarf
$0.08M_{\odot} < M < 0.5M_{\odot}$	Central hydrogen burning Formation of a degenerate core No helium ignition <b>Helium white dwarf</b>
$0.5M_{\odot} < M < 2M_{\odot}$	Central hydrogen burning Helium flash <b>CO white dwarf</b>
$2M_{\odot} < M < 8M_{\odot}$	Central hydrogen burning Helium ignites in nondegenerate core <b>CO white dwarf</b>
$8M_{\odot} < M < 20M_{\odot}$	Numerous burning phases Bulk of heavy element enrichment from $M > 10M_{\odot}$ Type II supernova <b>Neutron star</b>
$M > 20M_{\odot}$	<b>Black hole</b>

## Calculated evolutionary tracks

Data from Schaller et al., A&A Sup. Ser., 96, 269 (1992). Tracks for  $1M_{\odot}$ ,  $7M_{\odot}$ ,  $20M_{\odot}$ .



Solid lines show track during, core hydrogen burning, helium burning and carbon burning respectively.

Note different evolution of low mass and higher mass stars once they leave the main sequence. Several reasons,

- Low mass stars have no convective core  $\rightarrow$  continuous gradient in composition in central regions.
- Low mass stars have cores that are closer to the degeneracy boundary than high mass stars  $\rightarrow$  less evolution needed to create a degenerate core.
- Low mass stars are closer to the Hayashi line.

Dividing line at around  $2.3M_{\odot}$ .

Basic evolution involves,

- Contraction of the core, accompanied by expansion of the envelope.
- $\rightarrow$  reduced  $T_e$ , increased  $L$ .
- Sometimes repeated crossings of the HR diagram during He burning.

## Evolution past critical core mass

For a core composed of an ideal gas, used the virial theorem to derive an expression for the core pressure  $P_s$  as a function of core radius  $R_c$ .

Found that there was a maximum in this function  $\rightarrow$  maximum core mass that can match smoothly onto an envelope.

For small  $R_c$ , onset of degeneracy provides additional pressure support. In non-relativistic regime,

$$P \propto \rho^{5/3},$$

and taking core density  $\rho \propto M_c/R_c^3$  we obtain,

$$P = \frac{C_4 M_c^{5/3}}{R_c^5}.$$

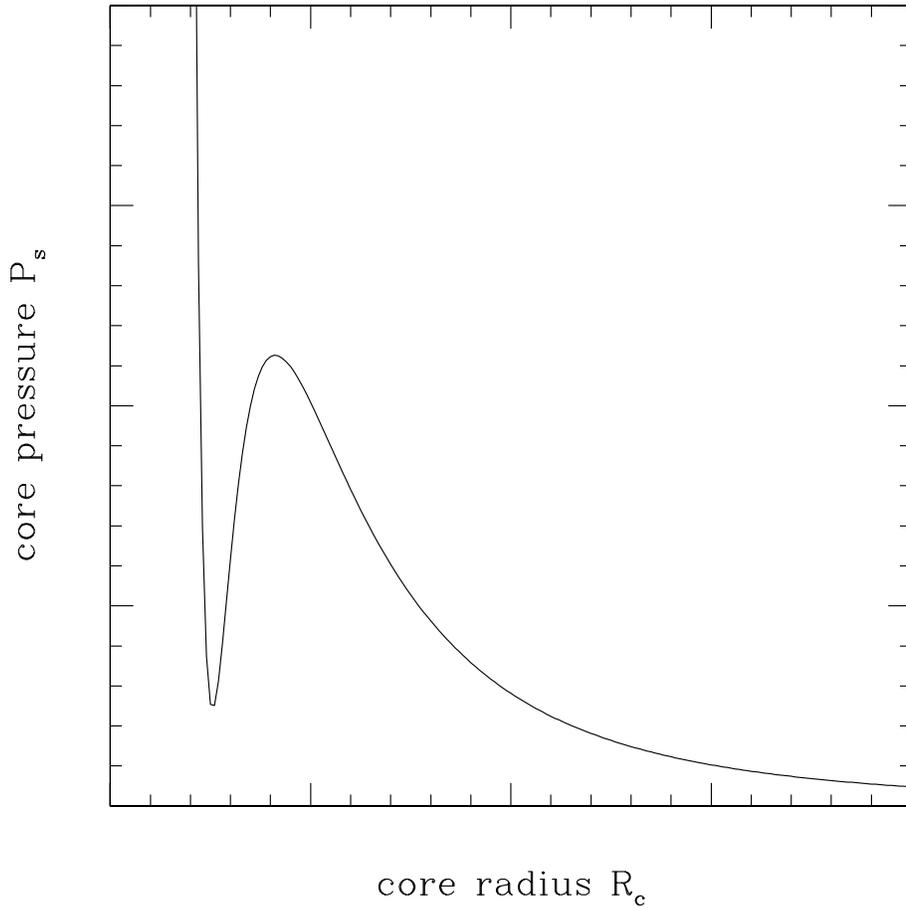
Adding this in to our previous expression, obtain,

$$P_s = \frac{C_1 M_c T_c}{R_c^3} - \frac{C_2 M_c^2}{R_c^4} + \frac{C_4 M_c^{5/3}}{R_c^5}.$$

Third term rises for small  $R_c \rightarrow$  allows star to find solution with degenerate core which does not exist if the core is assumed to remain an ideal gas.

If  $M_c$  is large enough, this function has two turning points.

Note: straightforward but not much gained by adding in the various constants.



As before, need to match  $P_s$  onto the envelope pressure, which is a straight line in this diagram.

Evolution for a star with  $M > 3M_{\odot}$  has three phases,

- Initially,  $q < q_{SC}$ . One, stable solution corresponding to a large, non-degenerate core.
- As  $q$  increases, reach a point where there are 3 possible solutions. Middle solution is thermally unstable, others represent a degenerate or non-degenerate core holding up the envelope. Continuity suggests we remain on the ‘large  $R_c$ ’ branch.
- When  $q$  exceeds  $q_{SC}$ , only solution corresponds to the degenerate core. Star must make a rapid transition to this structure.

Timescale for core contraction will be the Kelvin-Helmholtz time,

$$t_{KH} = \frac{GM^2}{RL}.$$

This timescale is short  $\sim 10^6$  yr for a star with  $M = 5M_{\odot}$ . Therefore few stars are observed populating the transition from high to low  $T_e \rightarrow$  this region in the HR diagram is the **Hertzprung gap**.

Easy to see why the core must contract. Numerical calculations show that this is accompanied by an expansion of the envelope. Numerous explanations, mostly of questionable validity, for why this should be so.

Example from Padmanabhan:

Consider timescales shorter than the Kelvin-Helmholtz time. Both energy conservation,

$$\Omega + U = \text{constant}$$

and the virial theorem,

$$\Omega + 2U = \text{constant}$$

must hold over such timescales. Thus,  $\Omega$  and  $U$  must be conserved separately.

For  $M_c \gg M_{env}$ ,

$$|\Omega| \approx \frac{GM_c^2}{R_c} + \frac{GM_c M_{env}}{R}$$

where  $R$  is the radius of the star and we have assumed that the binding energy of the envelope is dominated by the gravity of the core.

If we take  $M_c$  to be constant (hence  $M_{env}$  also) then,

$$-\frac{GM_c^2}{R_c^2} \frac{dR_c}{dt} - \frac{GM_c M_{env}}{R^2} \frac{dR}{dt} = 0$$

which implies,

$$\frac{dR}{dR_c} = - \left( \frac{M_c}{M_{env}} \right) \left( \frac{R}{R_c} \right)^2$$

ie the envelope expands as the core contracts.

Lengthy discussions of ‘why stars become red giants’ can be found in the literature,

- Iben, ApJ, 415, 767 (1993), ‘*the transition from main sequence to giant branch involves a complicated interplay between a core, an envelope, and a nuclear-burning shell*’.
- Renzini & Ritossa, ApJ, 433, 293 (1994), expansion is driven by increased opacity in the envelope.
- Laughlin, Bodenheimer & Adams, ApJ, 482, 420 (1997), expansion is due to (1) increased core luminosity, (2)  $\mu$  gradients, (3) atmospheric opacity.

Difficulty is in finding an intuitive explanation – numerical results are clear and in general agreement with observations.

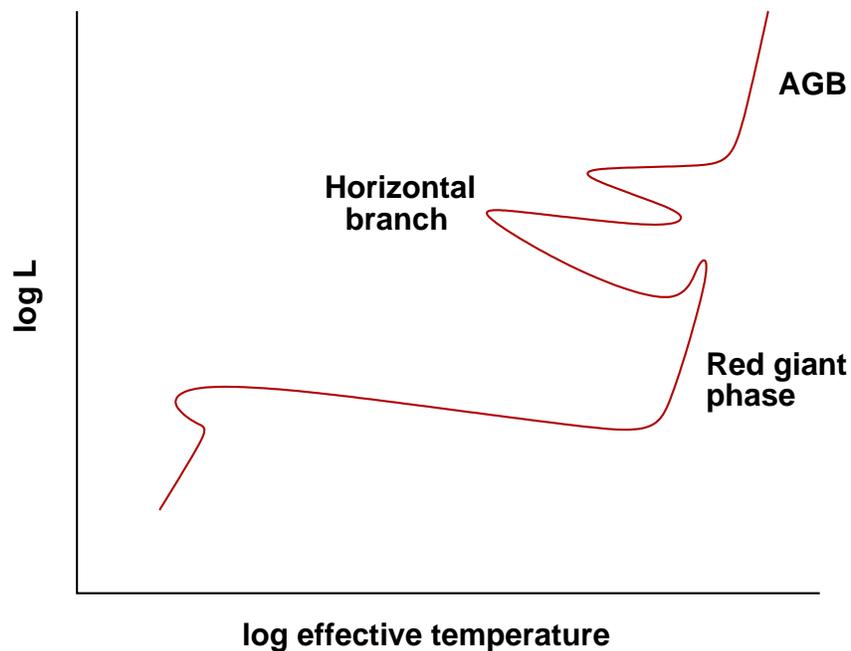
Once the envelope has expanded, opacity in the photosphere increases due to  $H^-$  in the outer regions  $\rightarrow$  establishment of a surface convection zone.

Near vertical evolution along a Hayashi track.

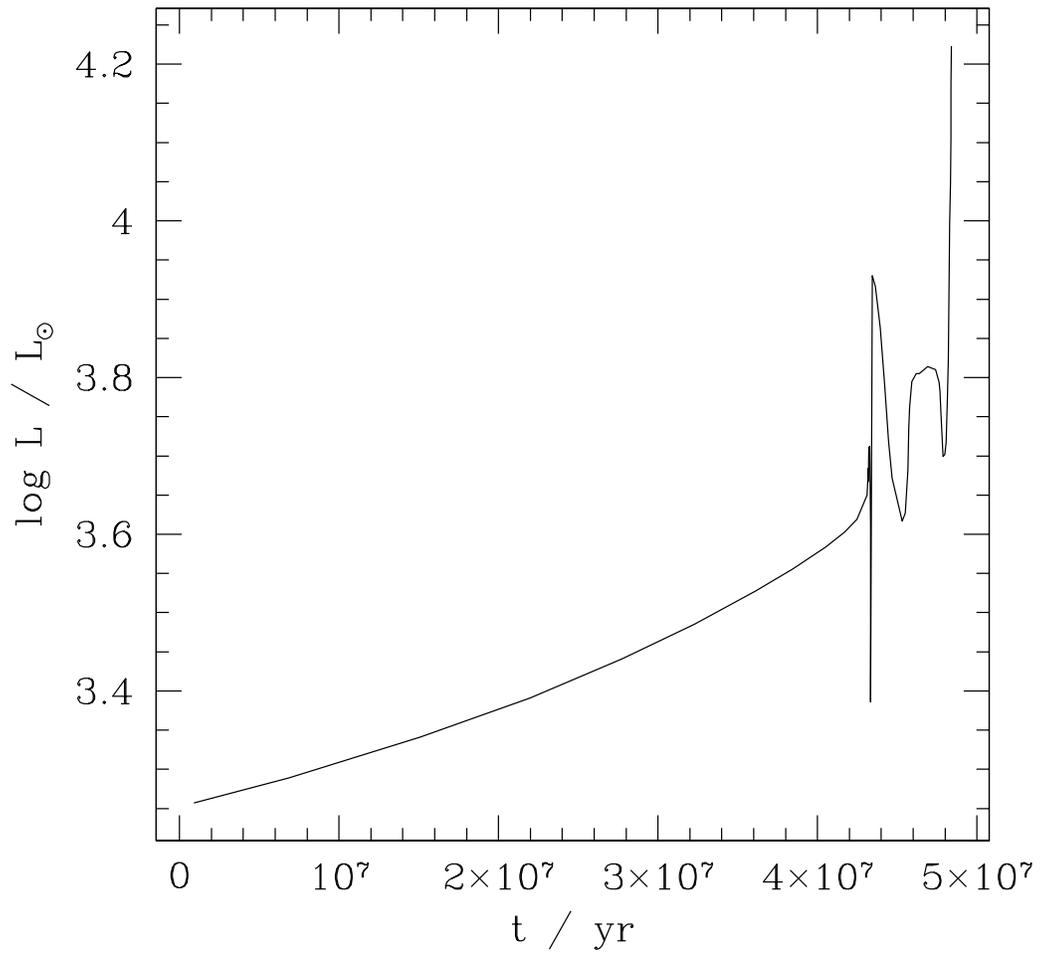
Convection zone can be deep enough to retrieve products of nuclear burning '**dredge-up**'.

Onset of helium burning in the core (plus hydrogen burning in a shell) leads to an excursion to higher  $T_e$ . The **horizontal branch**.

Next phase of Hayashi track evolution when core helium burning ceases is the **asymptotic giant branch**.



Calculated luminosity evolution for  $7 M_{\odot}$ :



Calculated radius evolution for  $7 M_{\odot}$ :

